

*Consequences of
Population Structure*

Biostatistics 666

Sources of Association

- Causal association

best

- Genetic marker alleles influence susceptibility

- Linkage disequilibrium

useful

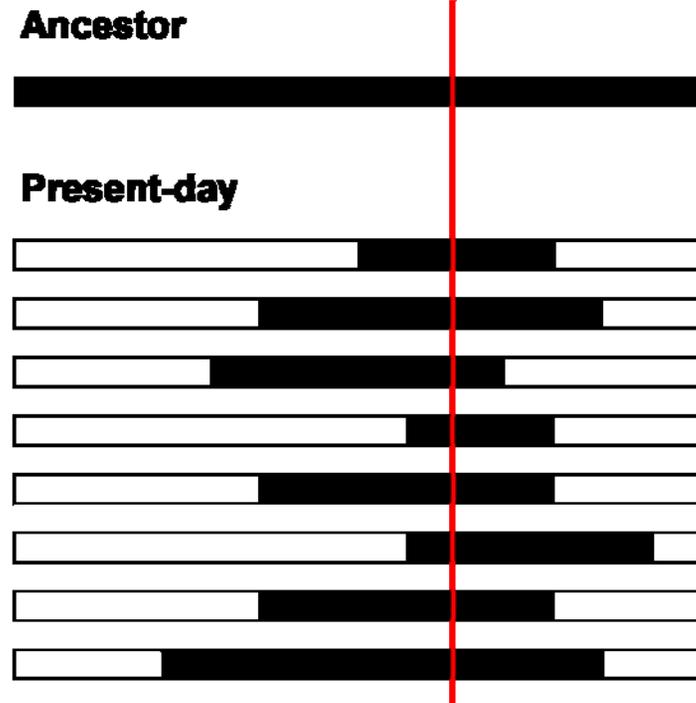
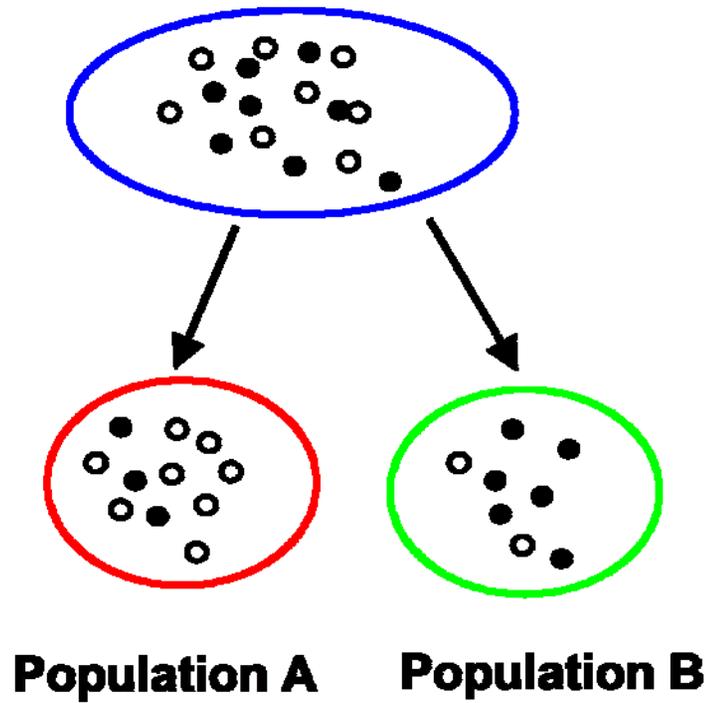
- Genetic marker alleles associated with other nearby alleles that influence susceptibility

- Population stratification

misleading

- Genetic marker is unrelated to disease alleles

Stratification vs Disequilibrium



Impact of Stratification at One Locus – Numerical Example

	<u>Sample</u>		
	Population 1	Population 2	Combined
<u>Allele Frequencies</u>			
P ₁	0.20	0.80	0.50
P ₂	0.80	0.20	0.50
<u>Genotype Frequencies</u>			
P ₁₁	0.04	0.64	0.34 (0.25 expected)
P ₁₂	0.32	0.32	0.32 (0.50 expected)
P ₂₂	0.64	0.04	0.34 (0.25 expected)

Notice the excess of homozygotes and deficit of heterozygotes.

Impact of Stratification at Two Loci – Numerical Example

Population A

	B ₁	B ₂
A ₁	160	160
A ₂	40	40

chi² = 0.0

Population B

	B ₁	B ₂
A ₁	160	40
A ₂	160	40

chi² = 0.0

Combined Population

	B ₁	B ₂
A ₁	320	200
A ₂	200	80

chi² = 7.83

The Stratification Problem

- If phenotypes differ between populations
- And allele frequencies have drifted apart
- Unlinked markers exhibit association
- Not very useful for gene mapping!

Stratification

- Due to non-random mating
 - Eg. Mating based on proximity or culture
- Allele frequencies drift apart in each group
 - Eg. Allele frequency differences at many genes between African-Americans and Caucasians
- If disease prevalence also differs, association studies can produce misleading results
 - Eg. Glaucoma has prevalence of ~2% in elderly Caucasians, but ~8% in African-Americans

Possible solutions

- Collect a better matched sample
- Identify population groupings
 - Using self reported ethnicity or genetic markers
 - Carry out association analysis within each group
- Account for inflated false-positive rate
- Use family based controls

Family-Based Tests

- Use family information to define well-matched controls
- Distinguish “true” association from population stratification

Trio Families

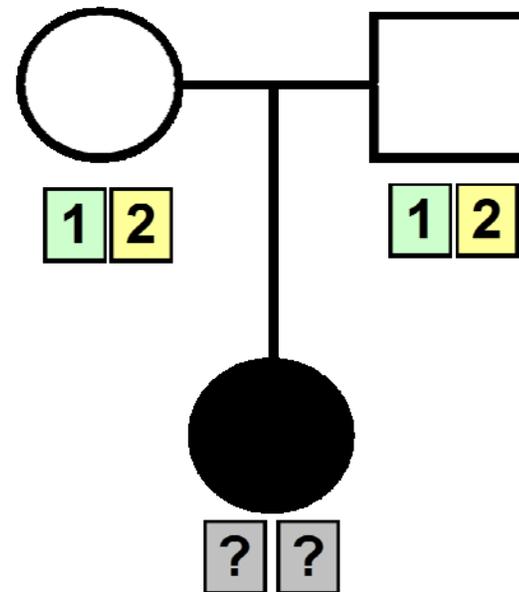
- Families with two genotyped parents
- One affected child
- Calculate distribution of child genotypes conditional on parental data
 - Focus on children with heterozygous parents

The Spielman TDT

- Traditional case-control
 - Compare allele frequencies in two samples
 - Cases and controls must be one population
- Heterozygous parents
 - Parental alleles are the study population
 - Population allele frequencies fixed
 - 50:50, independent of original
 - Check proportion of each allele transmitted to affected offspring

Basic TDT

- Is allele consistently transmitted from heterozygotes?
- Affirmative answer requires
 - Allele is associated
 - Allele is linked
 - Or we have a false-positive



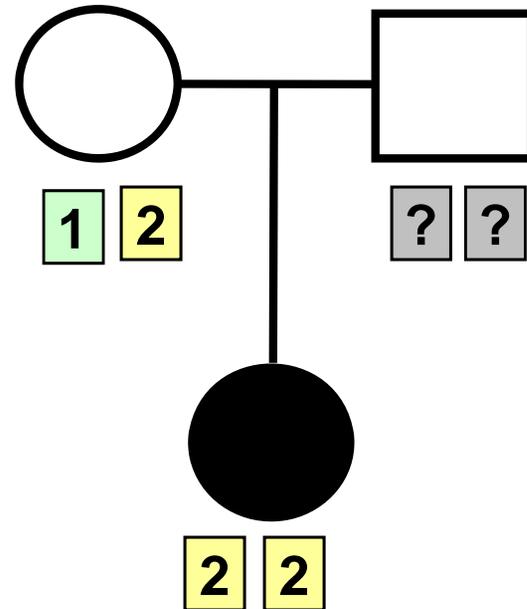
The TDT statistic

	Transmitted 1	Transmitted 2
Not-Transmitted 1	a	b
Not-Transmitted 2	c	d

$$\frac{(b - c)^2}{b + c} \sim \chi_1^2$$

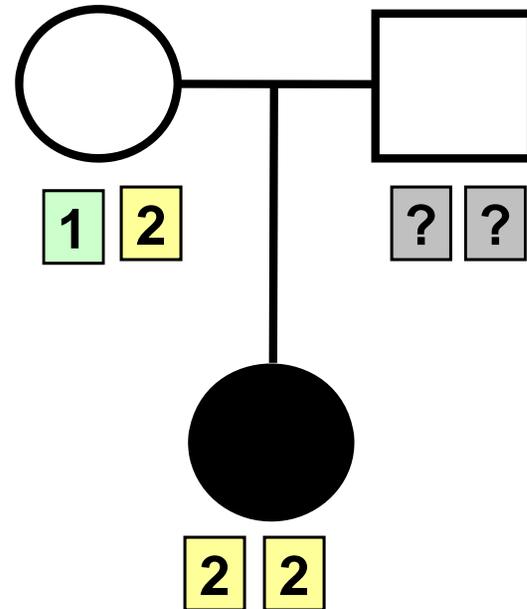
Caution: Parental genotypes crucial!

- It seems we can deduce transmitted allele...
- However, this leads to bias...
 - Why?



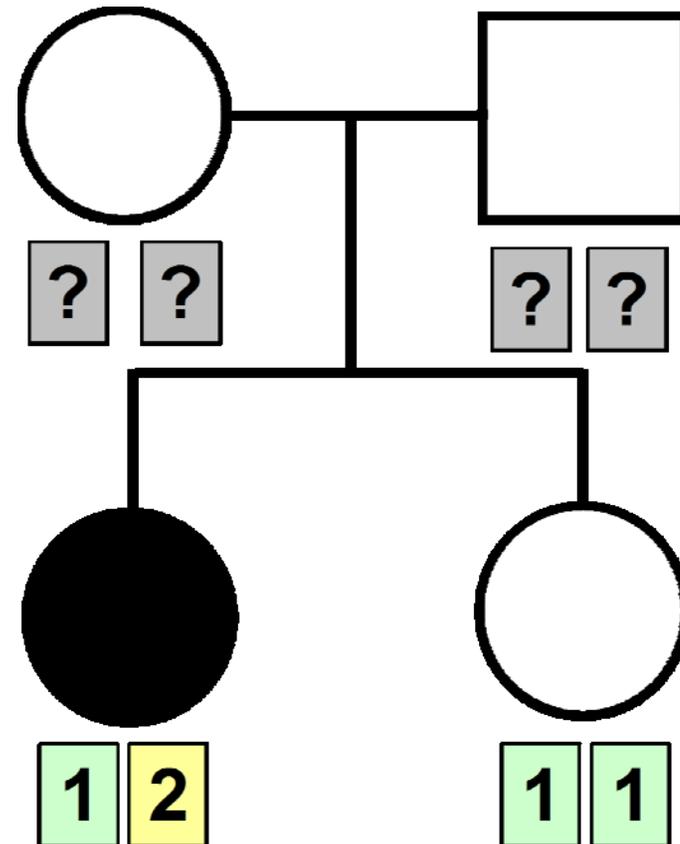
Caution: Parental genotypes crucial!

- Probability of inferring transmitted genotype depends on population allele frequencies
- Expected ratio of observed transmissions no longer 50/50.



The Sib-TDT

- Parents may be missing
 - eg. late onset conditions
- Compare alleles that differ between siblings
 - When sib genotypes differ, which allele is carried by affected sib?



The Sib-TDT statistic

	Affected has 1	Affected has 2
Unaffected has 1	a	b
Unaffected has 2	c	d

$$\frac{(b - c)^2}{b + c} \sim \chi_1^2$$

Further Extensions

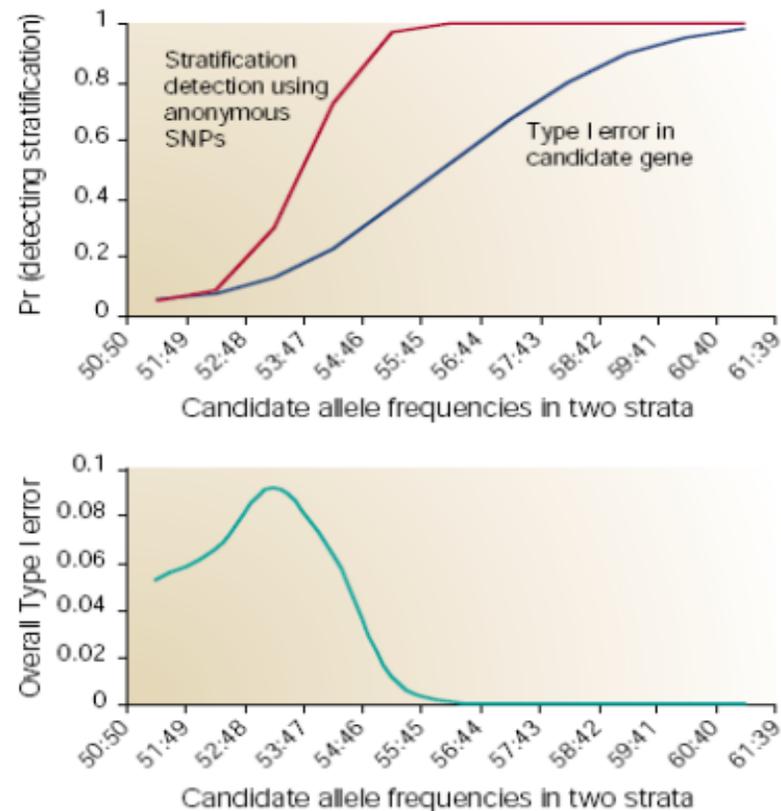
- The TDT can be further extended to model genotype, rather than allele, distributions
 - Schaid (1999) *Genet Epidemiol* **16**:250-260
- The TDT can be extended to accommodate different family structures

What if families are not available?

- Test null markers across genome
 - Markers that are unlikely to be associated
 - Markers that are outside genes
 - Markers in genes that are unlikely to be involved
- Initially, 50 markers suggested as minimum
- Now, typical to use 100,000 SNPs or more (from genomewide studies) as null

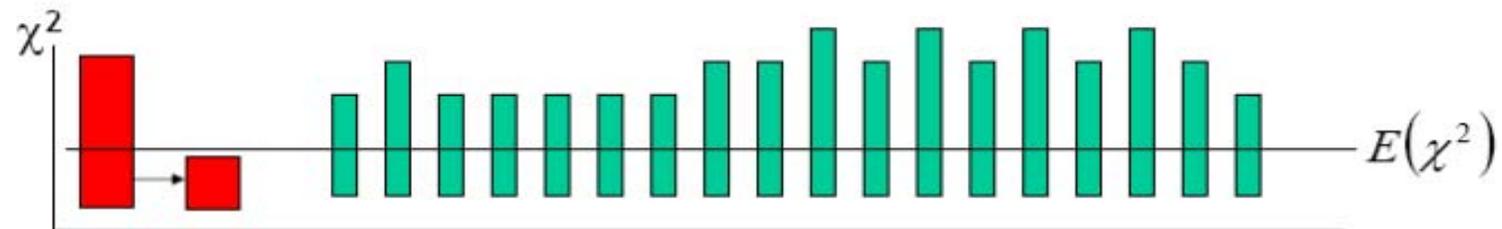
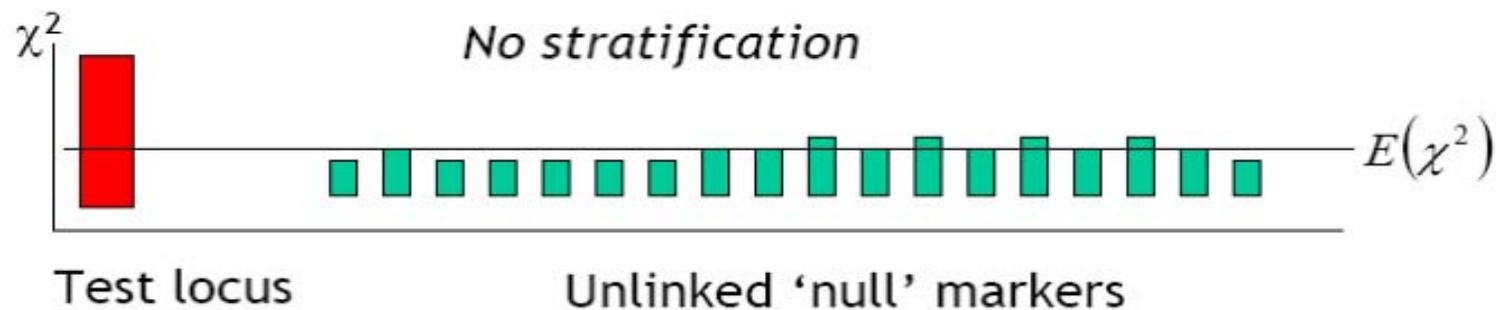
What if “null markers” reject null?

- Early suggestion:
 - Reject Association
 - Pritchard and Rosenberg (1999)
Am J Hum Genet
65:220-228
- What might be a better approach?



(Figure from Cardon and Bell, *Nature Reviews Genetics*, 2001)

Genomic Control



Stratification → adjust test statistic

(Figure courtesy Shaun Purcell, Harvard, and Pak Sham, HKU)

Define Inflation Factor

- Compute chi-squared for each marker
- Inflation factor λ
 - Average observed chi-squared
 - Median observed chi-squared / 0.456
 - Should be ≥ 1
- Adjust statistic at candidate markers
 - Replace χ^2_{biased} with $\chi^2_{\text{fair}} = \chi^2_{\text{biased}} / \lambda$

Questions

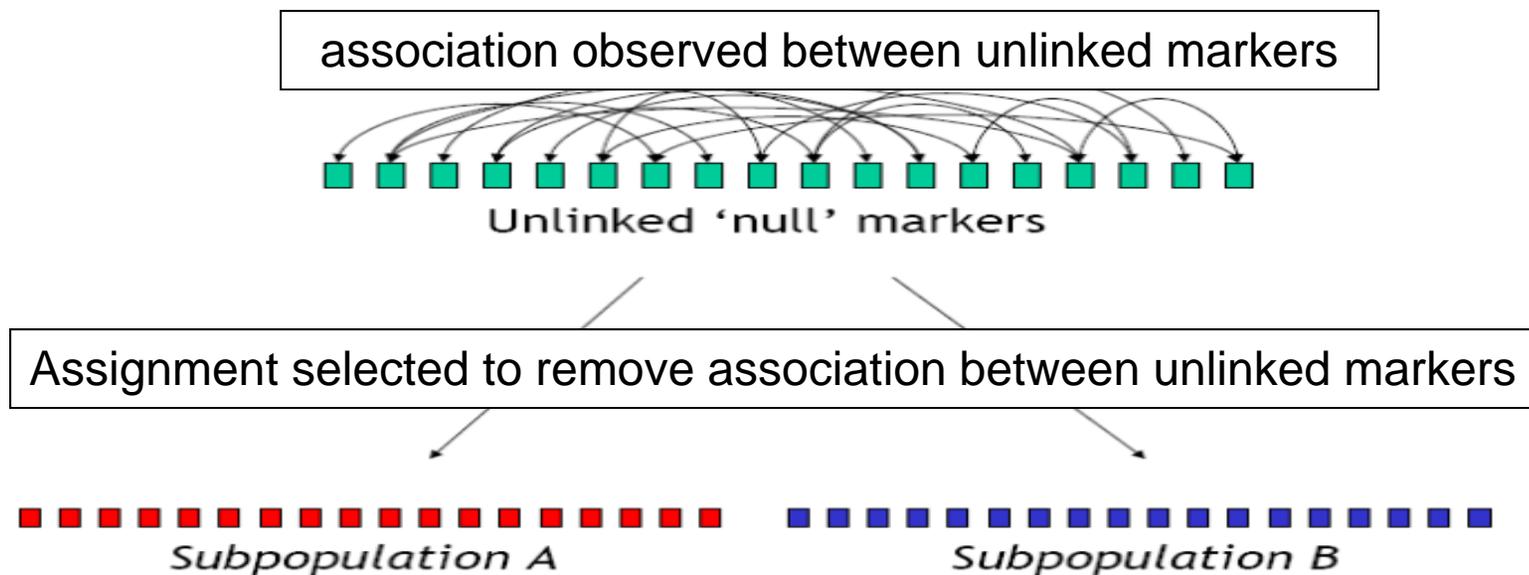
- When defining the inflation factor λ ...
- Why do we use a lower bound of 1?
- What might be the advantages of using the median rather than the mean?

Applying Genomic Control

- Simple and efficient method...
 - Easily adapted to other test statistics, such as those for quantitative trait and haplotype tests
- Under the null, stratification always inflates evidence for association...
 - Is this also true under the alternative?
 - What might be the consequences?

Structured Association

- Use unlinked markers to assign individuals to subpopulations then...
 - Test for association within each subpopulation
 - Test for association while conditioning on subpopulation



(Figure courtesy of Shaun Purcell and Pak Sham)

Some Attractive Features

- Allows for flexibility in association test
- Describing subpopulations can be useful
- Does not assume constant population differentiation across the genome

Simple Mixture Distribution

$$p(x|\boldsymbol{\pi}, \boldsymbol{\Phi}) = \pi_1 p(x|\phi_1) + \dots + \pi_k p(x|\phi_k)$$

- $p(\cdot)$ are the probability functions
- x are the observed genotypes
- π are the mixture proportions for subpopulations
- ϕ are allele frequencies for each subpopulation
- k is the number of components

Maximum Likelihood Approach

- Find the parameters that maximize the likelihood for the entire sample

$$L = \prod_j p(x_j | \boldsymbol{\pi}, \boldsymbol{\Phi})$$
$$\ell = \sum_j \log p(x_j | \boldsymbol{\pi}, \boldsymbol{\Phi})$$

- Prior for the allele frequencies may also be included in the likelihood
- Likelihood can be maximized using a Gibbs sampler or E-M algorithm

Classifying Individuals

- Let Z_j be the population membership for individual i

$$\Pr(Z_j = i | \boldsymbol{\pi}, \boldsymbol{\Phi}) = \pi_i$$

$$\Pr(Z_j = i | x_j, \boldsymbol{\pi}, \boldsymbol{\Phi}) = \frac{\pi_i p(x_j | \phi_i)}{\sum_l \pi_l p(x_j | \phi_l)}$$

- Results from the application of Bayes' theorem

Testing for Association

- Once individuals are classified, there is leeway in selecting association test:
 - Test within each subpopulation
 - Test within each subpopulation, then combine results
 - Use a test that conditions on population membership
 - e.g. a regression model with appropriate covariates

Refinements to the Model

- Allowing for admixture within individuals
- Setting up a prior for allele frequencies that favors similar frequencies across populations
- Allowing for different tiers of population structure

References

- Genomic Control for Association Studies
 - Devlin and Roeder (1999) *Biometrics* **55**:997-1004
 - Pritchard and Rosenberg (1999) *Am J Hum Genet* **65**:220-228
- Methods for Inferring Population Structure
 - Pritchard, Stephens and Donnelly, 2000. *Genetics* **155**:945-959
- Transmission Disequilibrium Tests
 - Spielman et al (1993) *Am J Hum Genet* **52**:506-16 (trios)
 - Curtis (1997) *Ann Hum Genet* **61**:319-33 (sibling pairs)